## $\mathbf{QUIZ} \ \mathbf{5}$

## **DIRECTIONS:**

- No papers, phones, calculators, or gadgets are permitted to be out during the quiz.
- Show all work, clearly and in order You will lose points if any of these instructions are not followed.

Questions	Points	Score
1	1	
2	2	
3	2	
Total	5	

**Problem 1:** (1 point) State the  $\epsilon$ -property.

For all  $\epsilon > 0$ , there exists  $m \in \mathbb{N}$  such that  $\frac{1}{m} < \epsilon$ .

**Problem 2:** (2 points) For any poset  $(A, \leq)$  and subset  $B \subseteq A$ , prove that B has at most one least upper bound, lub(B)

**Proof:** Suppose L and L' are both least upper bounds of B. Then by the definition of least upper bound  $L \leq L'$  and  $L' \leq L$ . Hence L = L'.

Q.E.D.

Problem 3: (2 points) Label the following true or false

(a) (0.5 points) <u>F</u> A relation,  $\sim$ , on a set A that yields a poset  $(A, \sim)$  is a special kind of equivalence relation. That is it is reflexive, symmetric, and transitive.

(b) (0.5 points) \_\_\_\_ F \_\_\_  $\mathbb{Q}$  has the greatest lower bound property.

(c) (0.5 points) <u>T</u>  $\mathbb{R}$  is a complete ordered field.

(d) (0.5 points) <u>F</u> If an ordered field, F, has the greatest lower bound property, then any non-empty subset  $B \subseteq F$  has a greatest lower bound.