

MATH 237: Vector Calculus

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1. Consider the curves traced out by the vector-valued functions

$$\mathbf{s}(t) = \langle 13, 2, 4 \rangle + t\langle 5, 3, \sqrt{7} \rangle \quad 0 \leq t \leq 1$$

and

$$\mathbf{r}(t) = \langle \cos t, \sin t, t \rangle, 0 \leq t \leq 2\pi$$

- (a) What are the lengths of these curves?

- (b) Can you redescribe the curves so that the distance traveled is the same as the time interval?

2. Find the length of the curve traversed by

$$\mathbf{r}(t) = \langle t, \frac{\sqrt{2}}{2}t^2, \frac{1}{3}t^3 \rangle \quad 0 \leq t \leq 3\sqrt{2}$$

3. Find the average value of the function $T(x, y, z) = x^2y^2z^2$ along the curve above.