Convolution Integrals

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Say we have a Laplace transform which is a product of two simpler functions and we know the inverse Laplace transform of these two simpler functions.

That is, we have

$$H(s)=F(s)G(s),$$

where we know $f(t) = \mathcal{L}^{-1}(F(s))$ and $g(t) = \mathcal{L}^{-1}(G(s))$.

How can we use this information to find $h(t) = \mathcal{L}^{-1}(H(s))$?

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Convolution Integrals

$$\mathcal{L}^{-1}(H(s)) = \mathcal{L}^{-1}(F(s)G(s)) = \int_0^t f(t)g(t-\tau)d\tau.$$

The resulting function is called the **convolution product** of f and g and is denoted by f * g.

That is,

$$(f*g)(t)=f(t)*g(t)=\int_0^t f(t)g(t-\tau)d\tau.$$

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