

$$1. \vec{r}(t) = t^2 \vec{i} + \sin 2t \vec{j} + \cos 2t \vec{k}$$

$$\vec{r}'(t) = 2t \vec{i} + 2\cos 2t \vec{j} - 2\sin 2t \vec{k}$$

$$\|\vec{r}'(t)\| = \sqrt{4t^2 + 4} = 2\sqrt{t^2 + 1} = \frac{ds}{dt}$$

$$\vec{T}(t) = \frac{\vec{r}'(t)}{\frac{ds}{dt}} = \frac{t}{\sqrt{t^2 + 1}} \vec{i} + \frac{\cos 2t}{\sqrt{t^2 + 1}} \vec{j} - \frac{\sin 2t}{\sqrt{t^2 + 1}} \vec{k}$$

$$\vec{T}'(t) = \frac{(t^2 + 1)^{\frac{1}{2}} - t \cdot \frac{1}{2}(t^2 + 1)^{-\frac{1}{2}} \cdot 2t}{t^2 + 1} \vec{i} + \frac{-2\sin 2t \sqrt{t^2 + 1} - \cos 2t \cdot \frac{1}{2}(t^2 + 1)^{\frac{1}{2}} \cdot 2t}{t^2 + 1} \vec{j}$$

$$- \frac{2\cos 2t \sqrt{t^2 + 1} - \sin 2t \cdot \frac{1}{2}(t^2 + 1)^{\frac{1}{2}} \cdot 2t}{t^2 + 1} \vec{k}$$

$$= \frac{1}{(t^2 + 1)^{\frac{3}{2}}} \vec{i} + \frac{-2(t^2 + 1)\sin 2t - t\cos 2t}{(t^2 + 1)^{\frac{3}{2}}} \vec{j} - \frac{2(t^2 + 1)\cos 2t - t\sin 2t}{(t^2 + 1)^{\frac{3}{2}}} \vec{k}$$

$$\|\vec{T}'(t)\| = \frac{1}{(t^2 + 1)^{\frac{3}{2}}} \sqrt{1 + 4(t^2 + 1)^2 + t^2} = \frac{\sqrt{(1 + t^2)(1 + 4(t^2 + 1))}}{(t^2 + 1)^{\frac{3}{2}}}$$

$$\kappa = \frac{\|\vec{T}'(t)\|}{\frac{ds}{dt}} = \frac{\sqrt{5 + 4t^2}}{(t^2 + 1) \cdot 2\sqrt{t^2 + 1}} = \frac{1}{2} \frac{\sqrt{5 + 4t^2}}{(t^2 + 1)^{\frac{3}{2}}}$$

$$\vec{r}'(t) = \langle 2t, 2\cos 2t, -2\sin 2t \rangle$$

$$\vec{r}''(t) = \langle 2, -4\sin 2t, -4\cos 2t \rangle$$

$$\|\vec{r}'' \times \vec{r}'\| = \sqrt{64 + 64t^2 + 16} = 4\sqrt{5 + 4t^2}$$

$$\vec{r}'' \times \vec{r}' = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 2t & 2\cos 2t & -2\sin 2t \\ 2 & -4\sin 2t & -4\cos 2t \end{vmatrix} = \vec{i}(-8) - \vec{j}(-8t\cos 2t + 4\sin 2t) + \vec{k}(-8t\sin 2t - 4\cos 2t)$$

$$2. \bar{r}(t) = t \cos t \bar{i} - t \sin t \bar{j} + t^2 \bar{k}$$

$$\bar{r}'(t) = (\cos t - t \sin t) \bar{i} + (-\sin t - t \cos t) \bar{j} + 2t \bar{k}$$

$$\begin{aligned} \|\bar{r}'(t)\| &= (\cos^2 t - 2t \cos t \sin t + t^2 \sin^2 t + \\ &\quad \sin^2 t + 2t \cos t \sin t + t^2 \sin^2 t + 4t^2)^{\frac{1}{2}} \\ &= \sqrt{1+5t^2} = \frac{ds}{dt} \end{aligned}$$

$$\bar{T}(t) = \frac{\cos t - t \sin t}{\sqrt{1+5t^2}} \bar{i} - \frac{\sin t + t \cos t}{\sqrt{1+5t^2}} \bar{j} + \frac{2t}{\sqrt{1+5t^2}} \bar{k}$$

$$\bar{T}'(t) = \text{UGH!}$$

$$\begin{aligned} \bar{r}''(t) &= (-\sin t - \sin t - t \cos t) \bar{i} + (\cos t - \cos t + t \sin t) \bar{j} + 2 \bar{k} \\ &= (-2 \sin t - t \cos t) \bar{i} + (t \sin t) \bar{j} + 2 \bar{k} \end{aligned}$$

$$\bar{r}' \times \bar{r}'' = \begin{vmatrix} \bar{i} & \bar{j} & \bar{k} \\ \cos t - t \sin t & -\sin t - t \cos t & 2t \\ -2 \sin t - t \cos t & t \sin t & 2 \end{vmatrix}$$

$$\begin{aligned} &= \bar{i} (-2 \sin t + 2t \cos t - 2t^2 \sin t) - \bar{j} (2 \cos t + 2t \sin t + 2t^2 \cos t) \\ &\quad + \bar{k} (-2 - t^2) \end{aligned}$$

$$\kappa = \frac{\|\bar{r}' \times \bar{r}''\|}{\left(\frac{ds}{dt}\right)^3} = \frac{\sqrt{8 + 16t^2 + 5t^4}}{(1+5t^2)^{3/2}}$$