

MATH 237 FALL 2016 Extra Questions

MATERIAL : 12.6,12.7,14.3

1. Give the critical points of the following:

(a)  $f(x, y, z) = yxz^2 + \ln\sqrt{x^2 + y^2}$  (b)  $w = ze^{-x^2-yz}$ .

2. Give the relative extrema and saddle points of the following

(a)  $f(x, y) = x^4 y^4 - 2x^2 y^2 + 8$  (b)  $z = 2x^2 + 8xy + 2y^2 - 6x + 8$  (c)  $f(x, y) = x^3 - 9xy + y^3$ .

3. Give the relative extrema of  $z = e^{x^2+y^2}$  for  $(x, y)$  on  $xy = 1$ .

4. Give the location of the relative extrema of  $f(x, y, z) = e^{x^2+y^2-z}$  on  $2x + 4y - 6z = 8$ .

5. Give the minimum distance from  $(0,1,2)$  to  $x^2 + y^2 - z = 4$ .

6. Give the dimensions of the box of maximum volume whose height plus area of the base is 32.

7. Give the surface areas of the following volumes: (a)  $z = 2r, 0 \leq z \leq 4$  (b)  $z = 9 - x^2 - y^2, z \geq 0$

(c)  $z = 18 - x^2 - y^2, x^2 + y^2 = 1, z \geq 0$  (d)  $z = 9 - x^2 - y^2$  and  $z = 1 + x^2 + y^2$

(e)  $x = 0, y = 0, z = 0$  and  $x + y + z = 3$ .