| Student: | Instructor: Josh Ducey | Assignment: Qualifier 2: Functions and |
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| Date: | Program: 199E: Precalculus/Algebra | Graphs |
| Time: |  |  |
|  | Gateway |  |
|  | Test Bank: MyMathTest: Basic Algebra, |  |
|  | Precalculus and Calculus |  |

1. Find the difference quotient of $f$; that is, find $\frac{f(x+h)-f(x)}{h}, h \neq 0$, for the following function. Be sure to fully simplify.
$f(x)=\sqrt{14 x}$
$\frac{\mathrm{f}(\mathrm{x}+\mathrm{h})-\mathrm{f}(\mathrm{x})}{\mathrm{h}}=\square$ (Simplify your answer.)
2. 

Find the difference quotient of $f$; that is, find $\frac{f(x+h)-f(x)}{h}, h \neq 0$, for the following function. Be sure to simplify.

$$
\begin{aligned}
& \frac{\mathrm{f}(\mathrm{x})=\mathrm{x}^{2}-6 \mathrm{x}+8}{\mathrm{f}(\mathrm{x}+\mathrm{h})-\mathrm{f}(\mathrm{x})} \mathrm{h}=\square \text { (Simplify your answer.) }
\end{aligned}
$$

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3. Use the graph to determine the following.
a. the function's domain
b. the function's range
c. the x -intercepts, if any
d. the $y$-intercept, if any
e. the function values, $f(-1)$ and $f(4)$.

Assume that the graph of the function
 continues its trend beyond the displayed coordinate grid.
a. What is the function's domain?
$\square$ (Type your answer in interval notation.)
b. What is the function's range?
(Type your answer in interval notation.)
c. Find the x -intercept(s), if there are any. Select the correct choice below and fill in any answer boxes within your choice.A. (Type an integer. Use a comma to separate answers as needed.)
B. There is no x -intercept.
d. Find the y-intercept(s), if there are any. Select the correct choice below and fill in any answer boxes within your choice.A. (Type an integer. Use a comma to separate answers as needed.)
B. There is no $y$-intercept.
e. Find the values of the function.

$$
\begin{aligned}
& \mathrm{f}(-1)=\square \\
& \mathrm{f}(4)=\square
\end{aligned}
$$

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4. 

Graph the rational function. Answer parts 1. through 6. below.

$$
f(x)=\frac{x^{2}+x-2}{x^{2}-16}
$$

1. Select the symmetry of the function.The function is symmetric about the $y$-axis.The function is symmetric about the origin.The function has no symmetry about the y-axis or the origin.
2. Find the y-intercept. Select the correct choice below and fill in any answer boxes within your choice.
A. The y-intercept is $\square$. (Type an integer or a simplified fraction.)B. There is no $y$-intercept.
3. Find any x-intercepts. Select the correct choice below and fill in any answer boxes within your choice.
A. The $x$-intercept(s) is/are $\square$.
(Type an integer or a simplified fraction. Use a comma to separate answers as needed.)B. There are no x -intercepts.
4. What are the x -coordinates of the vertical asymptote(s)? Select the correct choice below and fill in any answer boxes within your choice.$\mathrm{x}=$
(Use a comma to separate answers as needed.)B. There are no vertical asymptotes.
5. What is the y-coordinate of the horizontal asymptote? Select the correct choice below and fill in any answer boxes within your choice.

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4.$y=$
(cont.)B. There is no horizontal asymptote.
6. Using the information determined above, select the graph of the rational function.
○A


○


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5. Find the average rate of change of the function $f(x)=x^{2}+7 x$ from $x_{1}=1$ to $x_{2}=5$.

The average rate of change is $\square$ $\square$.

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6. Given the function $\mathrm{f}(\mathrm{x})=\sqrt{\mathrm{x}-8}$,
(a) Find $f^{-1}(x)$.
(b) Graph $f$ and $f^{-1}$ in the same rectangular coordinate system.
(c) Use interval notation to give the domain and the range of f and $\mathrm{f}^{-1}$.
(a) Find $f^{-1}(x)$.
$\mathrm{f}^{-1}(\mathrm{x})=\square ; \mathrm{x} \geq \square$
b) Choose the correct graph which shows $f$ and $f^{-1}$ graphed in the same coordinate system.
QA
A.

○в
○c

OD

(c) State the domain and range of $f$ and $f^{-1}$ using interval notation.

Domain of $\mathrm{f}=$ Range of $\mathrm{f}^{-1}=\square$
Range of $\mathrm{f}=$ Domain of $\mathrm{f}^{-1}=\square$
7.

The function $f(x)=\frac{5 x+4}{x-7}$ is one-to-one.

Find an equation for $\mathrm{f}^{-1}(\mathrm{x})$, the inverse function.
$\mathrm{f}^{-1}(\mathrm{x})=\square$
$\square$
(Simplify your answer. Use integers or fractions for any numbers in the expression.)

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8. Evaluate the function $f(x)=x^{2}-2 x+1$ at the given values of the independent variable and simplify.
a. $\mathrm{f}(-3)$
b. $f(x+8)$
c. $f(-x)$
a. $f(-3)=$
b. $f(x+8)=\square$
c. $\mathrm{f}(-\mathrm{x})=\square$
9. Use transformations of $f(x)=x^{2}$ to graph the following function.

$$
g(x)=(x+5)^{2}-1
$$

Use the graphing tool to graph the function.



$$
\begin{gathered}
\text { + } \triangle \vee C O C= \\
\text { Delete Clear }
\end{gathered}
$$


10. Use the graphs of f and g to evaluate the composite function.

$$
(f \circ g)(-1)
$$



$$
(f \circ g)(-1)=\square
$$

