

235 MIDTERM EXAM

You may use your notebook during the last fifteen minutes of this exam.

You may *NOT* use calculators, cell phones, loose papers, or peeking.

Small numbers to the right of the problems indicate similar homework exercises.

Math 235
November 5, 2012

Name: _____
By printing my name I pledge to uphold the honor code.

1. Determine whether each of the following is true or false. #1 all sections
- T F** If $f'(3) = 0$, then f has a local extremum at $x = 3$.
- T F** The inverse of $y = x^5$ is $y = x^{-5}$.
- T F** $\sec^{-1} x = \frac{1}{\cos^{-1} x}$.
- T F** If f is differentiable on \mathbb{R} and has an extremum at $x = -2$, then $f'(-2) = 0$.
- T F** For all real numbers x , there exists some real number y such that $x = y^2$.
- T F** $\frac{d}{dz}\left(\frac{1}{z}\right) = \ln z$.
- T F** If f is an exponential function, then f' is a constant multiple of f .
- T F** $0 < |x - c|$ if and only if $x \neq c$.
- T F** If a circle grows larger in such a way that its radius increases at a constant rate, then its circumference will also increase at a constant rate.
2. Which of the following is equal to the derivative of $f(x) = \sqrt{\ln(x^2 + 1)}$? 2.5 #36
- A)** $f'(x) = \frac{x}{(x^2 + 1)\sqrt{\ln(x^2 + 1)}}$ **C)** $f'(x) = (\ln(x^2 + 1))^{-\frac{1}{2}}(x)$
- B)** $f'(x) = \frac{1}{2}x^{-\frac{1}{2}}\left(\frac{1}{x^2+1}\right)$ **D)** $f'(x) = \frac{1}{2}\left(\frac{2x}{x^2+1}\right)^{-\frac{1}{2}}$
3. What important theorem is a key part of the proof of Rolle's Theorem? 3.1 reading
- A)** The Mean Value Theorem **C)** The Extreme Value Theorem
- B)** The Intermediate Value Theorem **D)** The Implicit Function Theorem

4. Which of the following is a function whose derivative is $f'(x) = \frac{e^x}{1 + e^x}$? 2.5 #63
- A) $f(x) = \tan^{-1}(\sqrt{e^x})$ C) $f(x) = \ln(1 + e^x)$
- B) $f(x) = \frac{e^x}{x + e^x}$ D) $f(x) = \frac{e^x(1 + e^x) + e^x(1 + e^x)}{(1 + e^x)^2}$
5. Calculate $\lim_{x \rightarrow -\infty} \frac{e^x}{\tan^{-1} x}$. Ch.1 rev #22
- A) $\frac{\pi}{2}$ B) ∞ C) 1 D) 0
6. Which of the four intervals I below is the largest interval on which we can guarantee that $x^2 \in (3.5, 4.5)$ for all $x \in I$? 1.2 #15
- A) (1.9, 2.1) C) (1.5, 2.5)
- B) $(2 - 3.5, 2 + 4.5)$ D) $(\sqrt{3.5}, \sqrt{4.5})$
7. Suppose that r is an independent variable, s is a function of r , and q is a constant. Calculate $\frac{d}{dr}(qs + r^2)$. 2.4 #56
- A) $q \frac{ds}{dr} + \frac{dq}{dr} s + 2r \frac{dr}{dr}$ C) $\frac{dq}{dr} \frac{ds}{dr} + 2 \frac{dr}{dr}$
- B) $q \frac{ds}{dr} + \frac{dq}{dr} s + (\frac{ds}{dr})^2$ D) $q \frac{ds}{dr} + 2r$
8. What is the domain of the function $\sqrt{(x - 1)(x + 2)}$? 1.1 #35
- A) $(-2, 1)$ C) $(-\infty, -2) \cup (1, \infty)$
- B) $[-2, 1]$ D) $(-\infty, -2] \cup [1, \infty)$
9. List all of the critical points of the function $f(x) = \frac{e^x}{x^2 - 3}$. 3.1 #33
- A) $x = 0, \pm 3$ B) $x = \pm\sqrt{3}$ C) $x = -1, 3, \pm\sqrt{3}$ D) $x = -1, 3$
10. Calculate $\lim_{h \rightarrow 0} \frac{(3 + h)^2 - 3^2}{h}$. 1.5 #64
- A) 6 B) 3 C) 9 D) 0

11. For which function does the second derivative test FAIL at $x = 0$? 3.3 #10
- A) $f(x) = x^4$ B) $f(x) = 3x + 1$ C) $f(x) = x^2$ D) $f(x) = x^2 + x^3$
12. Calculate $\lim_{x \rightarrow 1} \frac{\sin(\ln x)}{x - 1}$
- A) ∞ B) 0 C) $\frac{\pi}{2}$ D) 1
13. If f is differentiable and increasing on $[0, 5]$, then which is the largest? 2.1 #15
- A) $\frac{f(3) - f(1)}{2}$ C) Not enough information is given.
- B) $\lim_{h \rightarrow 0} \frac{f(1+h) - f(1)}{h}$ D) $\lim_{h \rightarrow 0} \frac{f(3+h) - f(3)}{h}$
14. If $\cos \theta = \frac{1}{5}$ and $\sin \theta < 0$, then what is $\sin \theta$? 0.4 #51
- A) $\frac{\sqrt{24}}{5}$ B) $\frac{1}{5}$ C) $\frac{2}{\sqrt{5}}$ D) $\frac{\sqrt{5}}{2}$
15. Suppose a rectangular ostrich pen is to be built with 540 feet of fencing material, and alongside a river (so that only three sides of fencing are required). Which of the following functions could be optimized in order to find the largest possible area of such a pen? 3.4 #36
- A) $f(x) = 2x + (540 - 2x)$ C) $f(x) = x(540 - 2x)$
- B) $f(x) = x(270 - x)$ D) $f(x) = 2x + \left(\frac{540}{x}\right)$
16. Which differentiation rule below did we prove WITHOUT using the definition of derivative? 2.3 reading
- A) $\frac{d}{dx}(\sin x) = \cos x$ C) $\frac{d}{dx}(\ln x) = \frac{1}{x}$
- B) $\frac{d}{dx}(f(x) + g(x)) = \frac{df}{dx} + \frac{dg}{dx}$ D) $\frac{d}{dx}(x^k) = kx^{k-1}$
17. Calculate $\lim_{x \rightarrow \infty} (x - \sqrt{x})$. 1.6 #39
- A) 0 B) \sqrt{x} C) ∞ D) $-\infty$

sCRAP

I will not be grading anything on this page but you must hand it in with your NAME: _____

BY COLORING INFINITY YOUR MIND BECOMES CLEAR:

